

# Branching Brownian motions in random environment

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We introduce a model of branching Brownian motions in random environment associated with the Poisson random measure in time-space. We then study the population growth rate and the diffusive behavior of this model. This talk is based on [S09-1] and [S09-2].

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