

988. Vector lattice, distributive law / 証明 = 就テ

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vector lattice, distributive law

$$(a \wedge b) \vee c = (a \vee c) \wedge (b \vee c)$$

ハ色々 + 証明ガアリマスガ、次ノ様ニスルト complete
ノ場合モ全時ニ簡單ニ証明出来マス。即チ

$$(\bigwedge_{\alpha} a_{\alpha}) \vee b = \bigwedge_{\alpha} (a_{\alpha} \vee b)$$

ヲ証明致シマス。

$$(\bigwedge_{\alpha} a_{\alpha}) \vee b \leq a_{\alpha} \vee b. \quad \text{ハ明カニ成立致シマス。}$$

總テ、 α ニ對シテ

$$x \leq a_{\alpha} \vee b$$

トスレバ

$$x \leq a_{\alpha} + b - a_{\alpha} \wedge b$$

$$x + a_{\alpha} \wedge b \leq a_{\alpha} + b$$

故ニ

$$\bigwedge_{\alpha} (x + a_{\alpha} \wedge b) \leq \bigwedge_{\alpha} (a_{\alpha} + b)$$

$$\text{即チ } x + (\bigwedge_{\alpha} a_{\alpha}) \wedge b = x + \bigwedge_{\alpha} (a_{\alpha} \wedge b) \leq \bigwedge_{\alpha} a_{\alpha} + b$$

$$\text{故ニ } x \leq \bigwedge_{\alpha} a_{\alpha} + b - (\bigwedge_{\alpha} a_{\alpha}) \wedge b = (\bigwedge_{\alpha} a_{\alpha}) \vee b$$

従ツテ

$$\circ (\bigwedge_{\alpha} a_{\alpha}) \vee b = \bigwedge_{\alpha} (a_{\alpha} \vee b)$$

トナリマス。

(1941, 11, 29)